

# ON QUASI-EINSTEIN MANIFOLDS

Ryszard Deszcz\*, Malgorzata Glogowska

*Wroclaw University of Environmental and Life Sciences, Department of Mathematics,  
Grunwaldzka 53, 50-357 Wroclaw, Poland*

[ryszard.deszcz@up.wroc.pl, malgorzata.glogowska@up.wroc.pl]

A semi-Riemannian manifold  $(M, g)$ ,  $n = \dim M \geq 3$ , is said to be an *Einstein manifold* if its Ricci tensor  $S$  is proportional to the metric tensor  $g$ , i.e.  $S = \frac{\kappa}{n} g$  holds on  $M$ , where  $\kappa$  is the scalar curvature. More generally,  $(M, g)$ ,  $n \geq 3$ , is called a *quasi-Einstein manifold* if at every point  $x \in M$  its Ricci tensor  $S$  satisfies  $\text{rank}(S - \alpha g) \leq 1$ ,  $\alpha \in \mathbb{R}$ , i.e. the condition  $S = \alpha g + \varepsilon w \otimes w$ ,  $\varepsilon = \pm 1$ ,  $w \in T_x^* M$ ,  $\alpha \in \mathbb{R}$ , holds at  $x$ . Quasi-Einstein manifolds arose during the study of exact solutions of the Einstein field equations and investigation in quasi-umbilical hypersurfaces of conformally flat spaces. In this talk we present results on quasi-Einstein warped product manifolds and quasi-Einstein hypersurfaces in space forms. Our talk bases on [1]-[7].

- [1] J. Chojnacka-Dulas, R. Deszcz, M. Glogowska and M. Prvanović, *On warped products manifolds satisfying some curvature conditions*, to appear.
- [2] F. Defever, R. Deszcz, M. Hotłoś, M. Kucharski and Z. Şentürk, *Generalisations of Robertson-Walker spaces*, *Annales Univ. Sci. Budapest. Eötvös Sect. Math.* **43** (2000), 13–24.
- [3] R. Deszcz, M. Glogowska, M. Hotłoś, and K. Sawicz, *A Survey on Generalized Einstein Metric Conditions*, in: *Advances in Lorentzian Geometry: Proceedings of the Lorentzian Geometry Conference in Berlin*, *AMS/IP Studies in Advanced Mathematics* **49**, S.-T. Yau (series ed.), M. Plaue, A.D. Rendall and M. Scherfner (eds.), 2011, 27–46.
- [4] R. Deszcz, M. Glogowska, M. Hotłoś and Z. Şentürk, *On certain quasi-Einstein semisymmetric hypersurfaces*, *Ann. Univ. Sci. Budap. Rolando Eötvös, Sect. Math.* **41** (1998), 151–164.
- [5] R. Deszcz and M. Hotłoś, *On hypersurfaces with type number two in spaces of constant curvature*, *Ann. Univ. Sci. Budap. Rolando Eötvös, Sect. Math.* **46** (2003), 19–34.
- [6] R. Deszcz, M. Hotłoś and Z. Şentürk, *On curvature properties of certain quasi-Einstein hypersurfaces*, *Int. J. Math.*, in print.
- [7] M. Glogowska, *On quasi-Einstein Cartan type hypersurfaces*, *J. Geom. Phys.* **58** (2008), 599–614.