

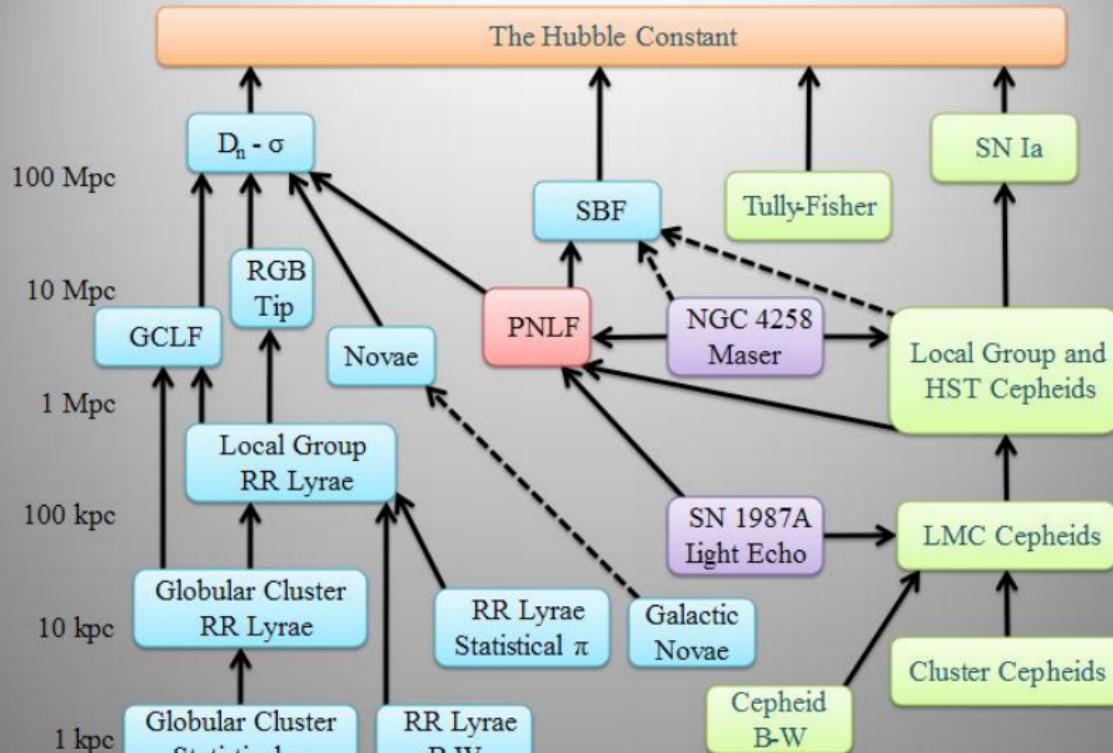
Fitovanje ili prebrojavanje: primer na uzorku planetarnih maglina

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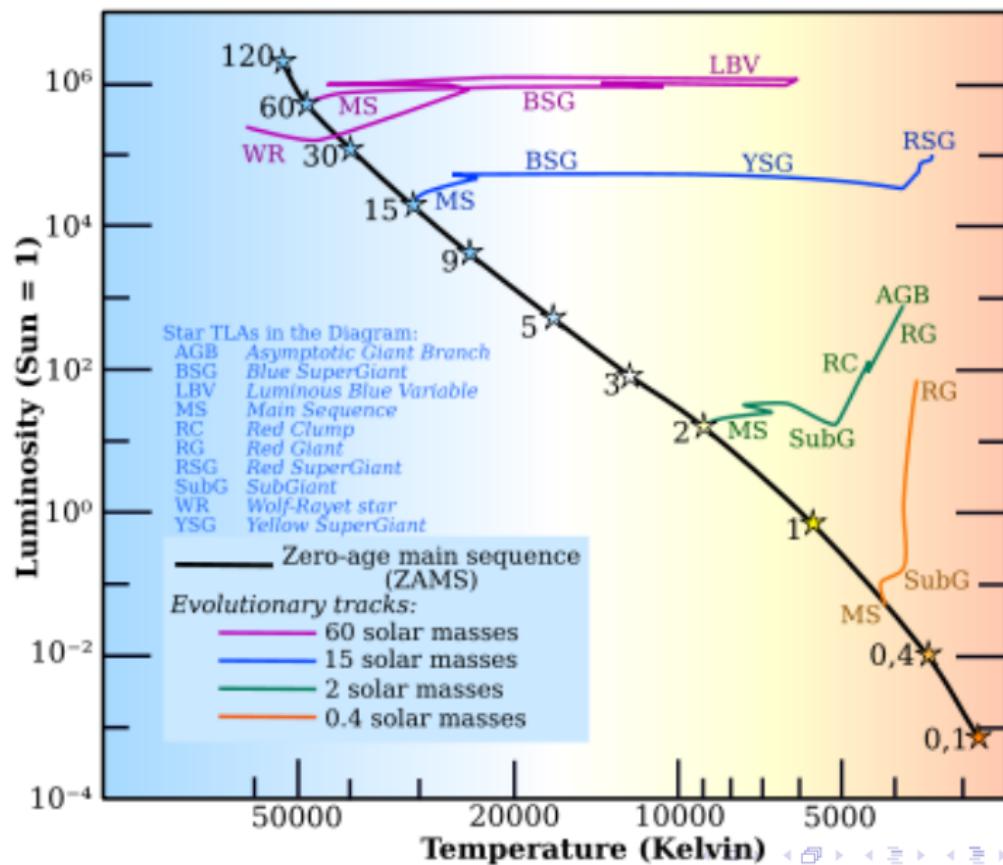
08.05.2012.

Daljine

Extragalactic Distance Ladder



"Planetarne" magline (AGB magline)



$\Sigma - D$ statističke daljine

Shklovsky, J.S, 1956, H_{β} emisija iz ionizovane ljudske koja se širi.



$$D = 149 \left[\frac{M^2 j_{\beta}(T)}{\epsilon j_{\beta}(T)} \right] \theta_r^{-3/5} S_{\beta}^{-1/5}$$

$$\Sigma_{\nu} = \frac{S_{\nu}}{\Omega}, \quad \Omega = \left(\frac{D}{d}\right)^2, \quad D = \theta d$$

$$\Sigma = AD^{\beta}$$

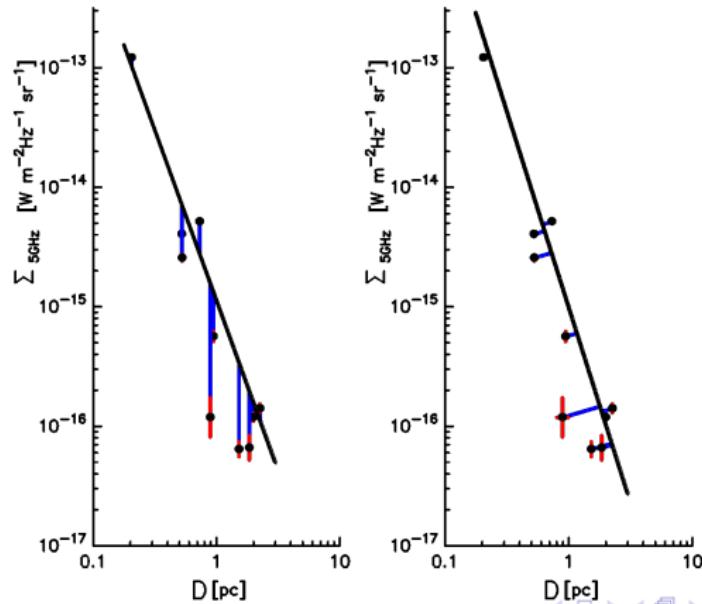
$$R - T_b \text{ i } \mu - \tau$$

Tip fita

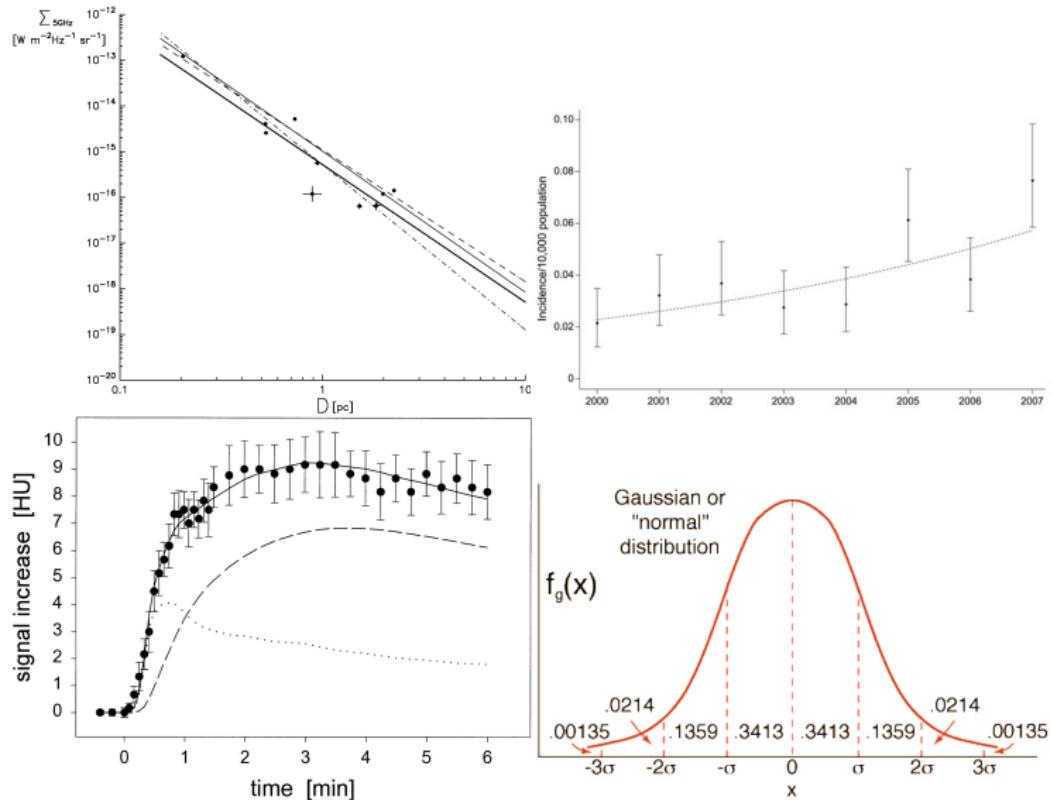
$$\Sigma = A'D^\beta, \quad D = B'\Sigma^\alpha$$

$$\log \Sigma = a + b \log D,$$

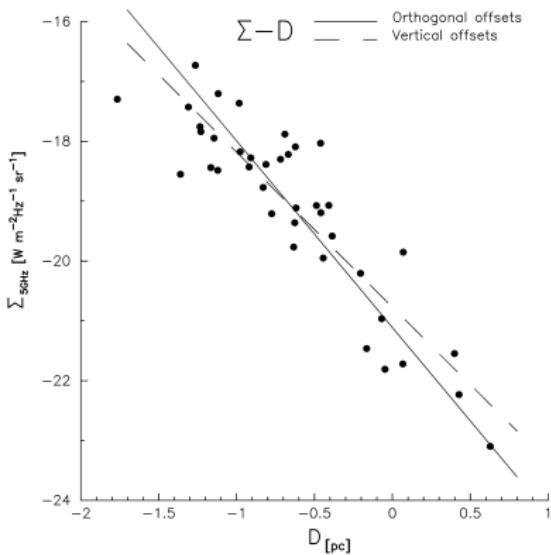
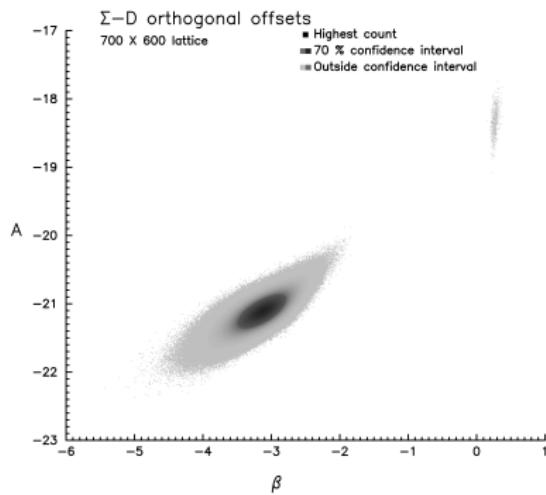
$$d = \frac{|y_i - a - bx_i|}{\sigma_{y_i}}, \quad d = \frac{|y_i - a - bx_i|}{(\sigma_{y_i}^2 + \sigma_{x_i}^2 b^2)^{0.5}}$$



Statistika fita.



Bootstrap i netežinsko fitovanje. Opet uz gubitak informacije.



$$\text{Vert: } A = -20.74, \quad \beta = -2.56, \quad ferr = 0.55.$$

$$\text{Perp: } A = -21.14, \quad \beta = -3.14, \quad ferr = 0.48.$$

Slučaj planetarnih maglina

Title: Shapes and Shaping of Planetary Nebulae

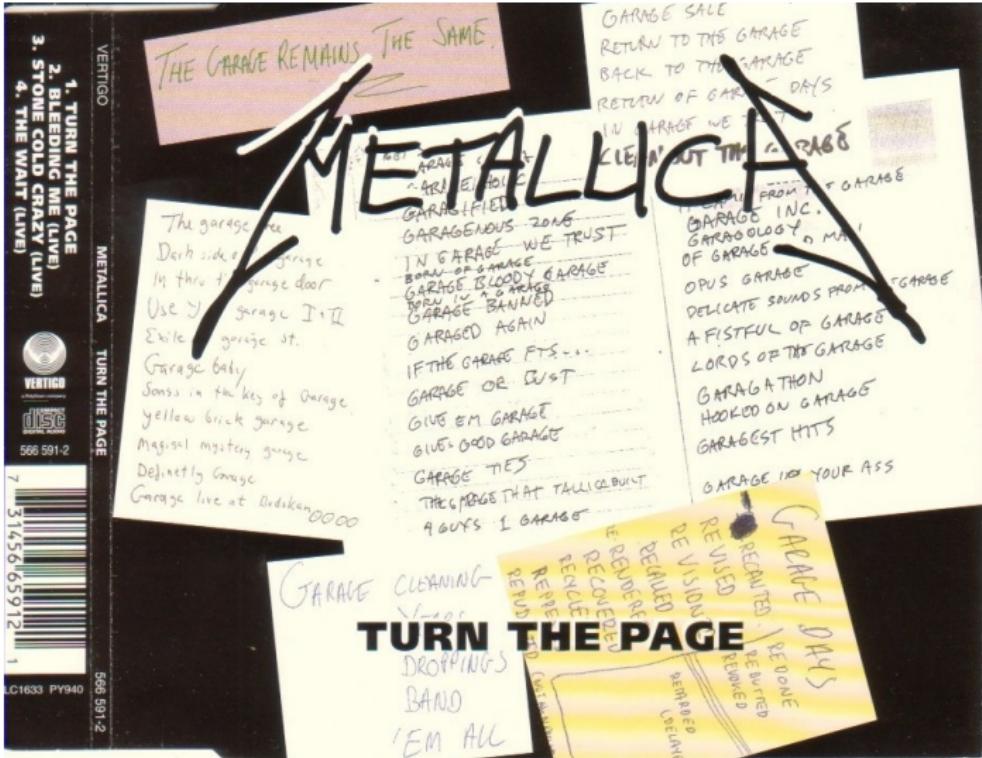
Authors: Balick, Bruce; Frank, Adam

Publication: Annual Review of Astronomy and Astrophysics, Vol. 40, p. 439-486 (2002) (Annual Reviews Homepage)

Abstract. We review the state of observational and theoretical studies of the shaping of planetary nebulae (PNe) and protoplanetary nebulae (pPNe). **In the past decade, high-resolution studies of PNe have revealed a bewildering array of morphologies with elaborate symmetries. Recent imaging studies of pPNe exhibit an even richer array of shapes. The variety of shapes, sometimes multiaxial symmetries, carefully arranged systems of low-ionization knots and jets, and the often Hubble-flow kinematics of PNe and pPNe indicate that there remains much to understand about the last stages of stellar evolution.** In many cases, the basic symmetries and shapes of these objects develop on extremely short timescales, seemingly at the end of AGB evolution when the mode of mass loss abruptly and radically changes. No single explanation fits all of the observations. The shaping process may be related to external torques of a close or merging binary companion or the emergence of magnetic fields embedded in dense outflowing stellar winds. We suspect that a number of shaping processes may operate with different strengths and at different stages of the evolution of any individual object.

Vreme je da se okreće list!

Bez potrebe za određivanjem greški tačaka, bez pp o tipu fita i bez gubitka informacije.

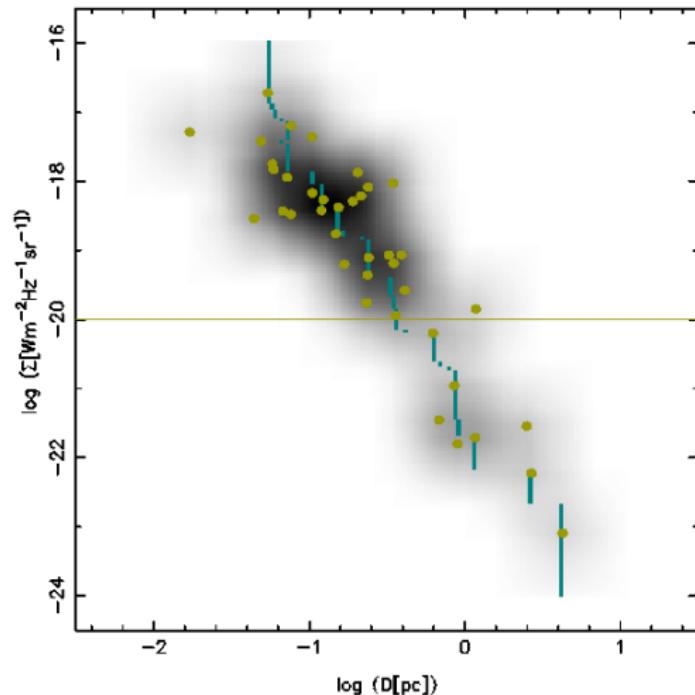


Kako?

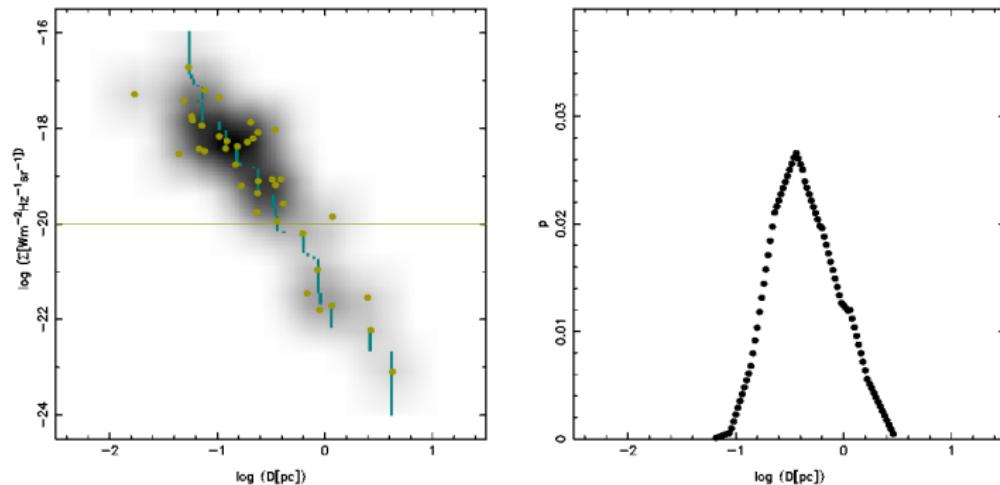
Prost frequency count u obliku histograma – Origin, ...

Problem kada ima malo tačaka.

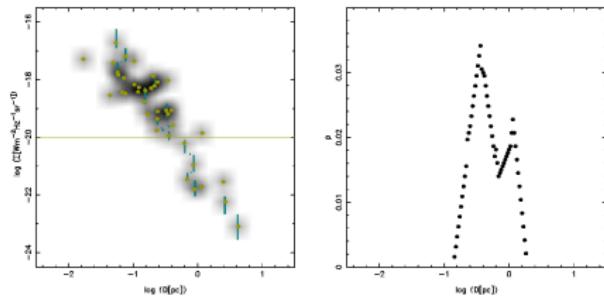
		b	b	b
	b	b	b	b
a	a	<a,b>		a
a	a	a		
a	a	a		



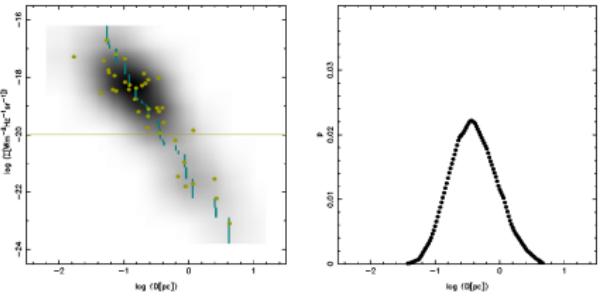
Određivanje dijametra



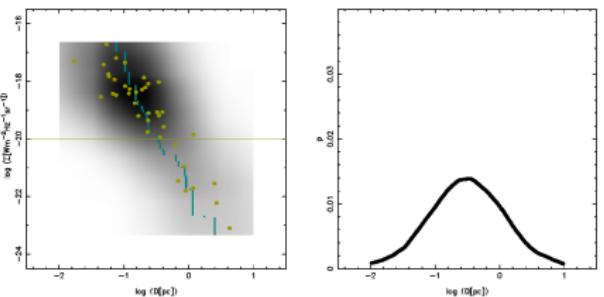
$$r = 10, ferr = 0.43$$



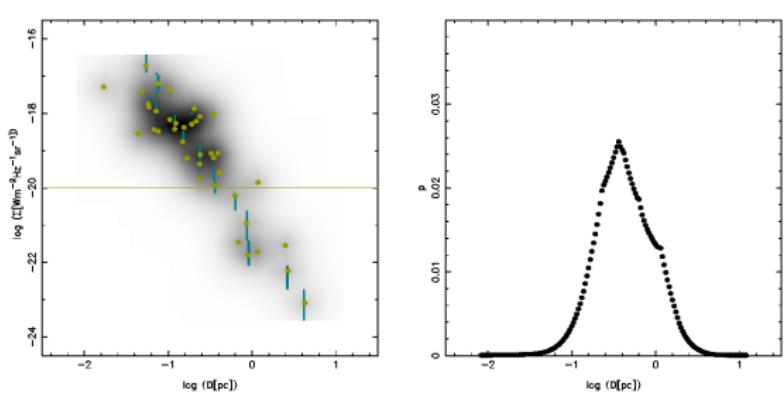
$r = 5, ferr = 0.47$



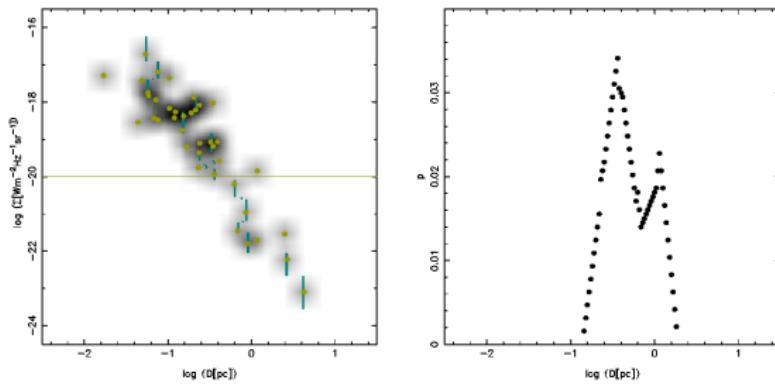
$r = 15, ferr = 0.42$



$r = 25, ferr = 0.60$



$r = 5-20, ferr = 0.41$



$r = 5, ferr = 0.47$

Za uraditi

- Uraditi prebrojavanje na „prirodnoj“ skali koja nije logaritamska.
- Naći postupak određivanja veličine okoline.
- ...